

EXAMPLE 7 Constructing Sequences

The second and fifth terms of a sequence are 3 and 24, respectively. Find explicit and recursive formulas for the sequence if it is (a) arithmetic

$$\underline{-4}, \underline{3}, \underline{10}, \underline{17}, \underline{24}$$

$$a_n = a_1 + (n-1)d$$

$$24 = 3 + (4-1)d$$

$$24 = 3 + 3d$$

$$21 = 3d$$

$$d = 7$$

$$a_n = -4 + (n-1)7$$

$$a_n = -4 + 7n - 7$$

$$a_n = 7n - 11$$

$$a_n = a_{n-1} + 7$$

EXAMPLE 7 Constructing Sequences

The second and fifth terms of a sequence are 3 and 24, respectively. Find explicit and recursive formulas for the sequence if it is **b) geometric**.

$$\frac{3}{2}, \frac{3}{1}, \frac{6}{1}, \frac{12}{1}, \frac{24}{1}, \frac{48}{1}$$

$a_n = \frac{3}{2}(2)^{n-1}$

$$a_n = a_{n-1}(2)$$

$$a_n = a_1 \cdot r^{n-1}$$

$$\frac{24}{3} = \frac{3}{3} \cdot (r)^{4-1}$$

$$8 = r^3$$

$$\sqrt[3]{8} = \sqrt[3]{r^3}$$

$$r = 2$$