Warm Up

Extract roots to rewrite each radical expression.

- 1. √48
- 2. √27
- 3. √32

1. Match each expression to an equivalent expression in the box. For each given expression, $a \neq 0$.



b.
$$\frac{a^3}{a^7}$$

c.
$$a^4 \cdot a^{-4}$$

d.
$$(ab^2)^2$$

e.
$$(a^2)^2$$

f.
$$\frac{a^6}{a^6}$$

g.
$$(a^8 b^4)^{\frac{1}{2}}$$

h.
$$a^2 \cdot a^{-6}$$

1

 a^4

 a^{-4}

 a^2b^4

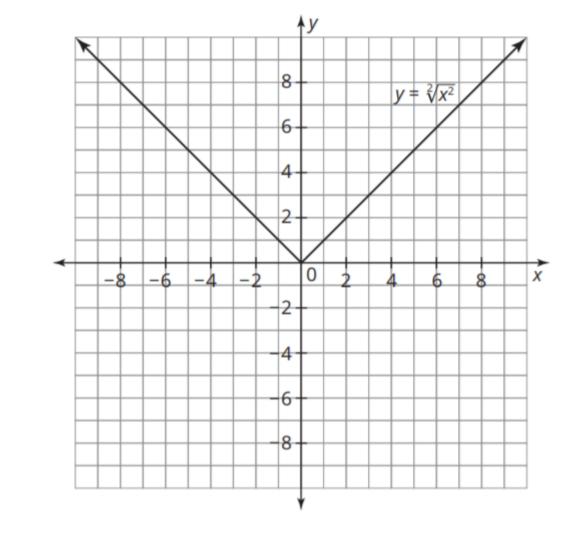
 a^4b^2



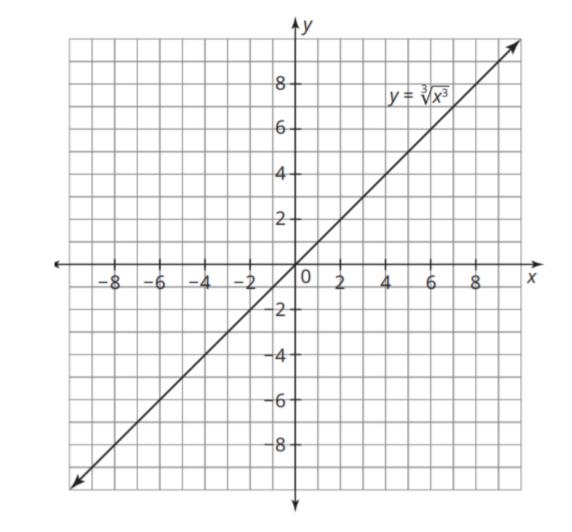
2. Jamal says that the expression $\frac{a^{\circ}}{a^{6}}$ is equivalent to 1 because any number, except 0, divided by itself is 1. Brittany says $\frac{a^{6}}{a^{6}}$ is equal to 1 because $a^{6-6} = a^{0}$, and anything to the zero power, except zero, equals 1. Who's correct? Explain your reasoning.

3. Consider each expression in Question 1. If a and b are real numbers, what do you know about the value of each expression? Explain your reasoning.

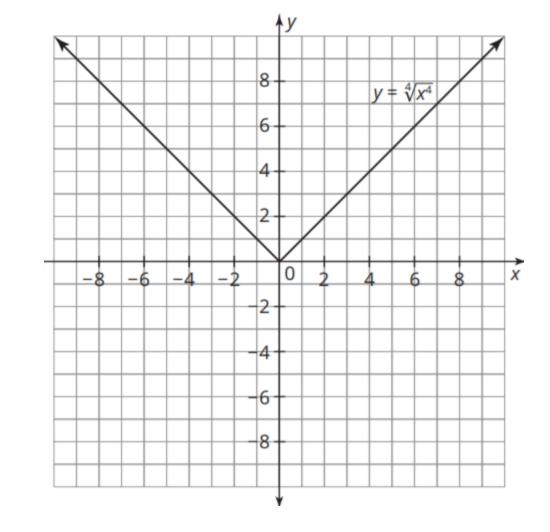
X	$\chi^n = \chi^2$	$\sqrt[n]{x^n} = \sqrt[2]{x^2}$
-2	4	2
-1	1	1
0	0	0
1	1	1
2	4	2



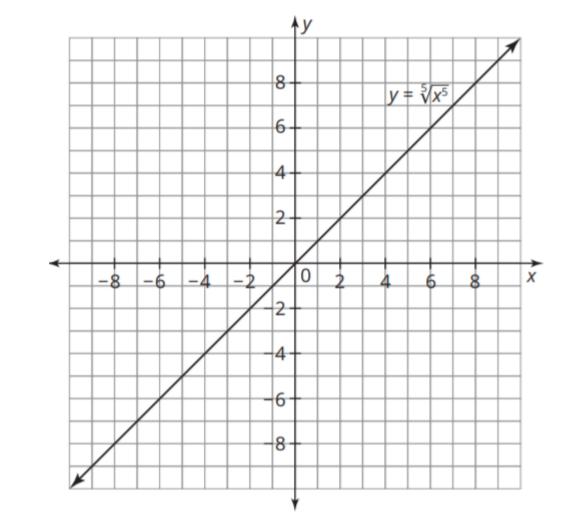
x	$\mathbf{x}^n = \mathbf{x}^3$	$\sqrt[n]{x^n} = \sqrt[3]{x^3}$
-2	-8	-2
-1	-1	-1
0	0	0
1	1	1
2	8	2



x	$\chi^n = \chi^4$	$\sqrt[n]{x^n} = \sqrt[4]{x^4}$
-2	16	2
-1	1	1
0	0	0
1	1	1
2	16	2



x	$\chi^n = \chi^5$	$\sqrt[n]{x^n} = \sqrt[5]{x^5}$
-2	-32	-2
-1	-1	-1
0	0	0
1	1	1
2	32	2



e. Analyze the representations for each value of *n*. What do you notice?

To extract a variable from a radical, the expression $\sqrt[n]{x^n}$ can be written as:

$$\sqrt[n]{x^n} = \begin{cases} |x|, \text{ when } n \text{ is even} \\ x, \text{ when } n \text{ is odd} \end{cases}$$

2. Explain why $\sqrt[7]{x^7} = |x|$ is incorrect, for real values of x.

One way to say $\sqrt[7]{x^7}$ is "the seventh root of x to the seven."



3. Asia and Melissa shared their work for extracting the root from $\sqrt{x^4}$, for real values of x.

Asia

$$\sqrt{x^4} = |x^2|$$

Melissa

$$\sqrt{X^4} = \sqrt{X^2 \cdot X^2}$$
$$= X^2$$

Who's correct? Explain your reasoning.